

The majority of the credit you receive will be based on the completeness and the clarity of your responses. Please use equal signs where appropriate and write solutions with a logical flow. Show your work, and avoid saying things that are untrue, ambiguous, or nonsensical.

1. Solve the following ODE's.

(a)  $\frac{dy}{dx} - y = e^{3x}$

(b)  $\frac{dy}{dx} = \frac{y}{x} + 2x + 1$

(c)  $\frac{dr}{d\theta} + r \tan \theta = \sec \theta$

(d)  $(x^2 + 1)\frac{dy}{dx} + xy = x$

2. Solve the following initial value problems.

(a)  $\frac{dy}{dx} - \frac{y}{x} = xe^x,$

$$y(1) = e - 1$$

(b)  $t^3 \frac{dx}{dt} + 3t^2 x = t,$

$$x(2) = 0$$

(c)  $\cos x \frac{dy}{dx} + y \sin x = 2x \cos^2 x,$

$$y\left(\frac{\pi}{4}\right) = \frac{-15\pi^2\sqrt{2}}{32}$$

3. Do Exercise #36 in Section 2.3.