

MATH 166
SUMMER 2011
QUIZ 14

1. (5 pt) Find the surface area generated when the function $f(x) = \sin(x)$, $0 \leq x \leq \pi$ is revolved about the x -axis.

2. (5 pt) A semicircular viewing window of radius R is constructed in an aquarium. This window is built so that the diameter of the window is incident with the surface of the water. Find the force due to hydrostatic pressure on this window (assume that water weighs ρ pounds per cubic foot).

Formulae

- (1) $\sin(2x) = 2 \sin(x) \cos(x)$
- (2) $\cos(2x) = \cos^2(x) - \sin^2(x)$
- (3) $\cos^2(x) = \frac{1}{2} + \frac{1}{2} \cos(2x)$
- (4) $\sin^2(x) = \frac{1}{2} - \frac{1}{2} \cos(2x)$
- (5) $\sin(A) \cos(B) = \frac{1}{2} [\sin(A - B) + \sin(A + B)]$
- (6) $\sin(A) \sin(B) = \frac{1}{2} [\cos(A - B) - \cos(A + B)]$
- (7) $\cos(A) \cos(B) = \frac{1}{2} [\cos(A - B) + \cos(A + B)]$
- (8) $e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!}$
- (9) $\sin(x) = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!}$
- (10) $\cos(x) = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n}}{(2n)!}$
- (11) $|E_M| \leq \frac{K(b-a)^3}{24n^2}$
- (12) $|E_T| \leq \frac{K(b-a)^3}{12n^2}$
- (13) $|E_S| \leq \frac{K(b-a)^5}{180n^4}$
- (14) $L = \int_a^b \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx = \int_a^b \sqrt{\left(\frac{dx}{dt}\right)^2 + \left(\frac{dy}{dt}\right)^2} dt = \int_a^b \sqrt{r^2 + \left(\frac{dr}{d\theta}\right)^2} d\theta$
- (15) $S = \int_a^b 2\pi(x \text{ or } y) ds$
- (16) $\int_{n+1}^{\infty} f(x) dx \leq R_n \leq \int_n^{\infty} f(x) dx$
- (17) $\bar{x} = \frac{1}{A} \int_a^b x(f(x) - g(x)) dx$
- (18) $\bar{y} = \frac{1}{2A} \int_a^b [(f(x))^2 - (g(x))^2] dx$
- (19) $A = \int_a^b \frac{1}{2} r^2 d\theta$
- (20) $\int \sec(x) dx = \ln |\sec(x) + \tan(x)| + c$
- (21) $\int \sec^3(x) dx = \frac{1}{2} \sec(x) \tan(x) + \frac{1}{2} \ln |\sec(x) + \tan(x)| + c$
- (22) If $t = \tan\left(\frac{x}{2}\right)$ then $\sin(x) = \frac{2t}{t^2+1}$, $\cos(x) = \frac{1-t^2}{t^2+1}$, $dx = \frac{2dt}{t^2+1}$