

**MATH 166**  
**SUMMER 2011**  
**QUIZ 3**

1. Consider the ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1; \quad a, b > 0.$$

- i) (5 pt) Find the volume obtained when the upper half of this ellipse is revolved about the  $x$ -axis.
- ii) (5 pt) Find the volume obtained when the right half of this ellipse is revolved about the  $y$ -axis.
- iii) (5 pt) What happens to your answers from i) and ii) when  $a = b$ ? Does this make sense? Why?

2. (5 pt) Find the volume obtained when the region bounded by  $f(x) = x$  and  $g(x) = x^n, n > 1$  is revolved about the line  $x = -1$ .

3. Suppose that we have a solid object whose volume at height  $x$  is given by

$$V(x) = \int_0^x A(t)dt.$$

- i) (5 pt) If the volume of this object is given by  $V(x) = \frac{4}{3}\pi x^3$ , determine the cross sectional area at height  $x$ .
- ii) (5 pt) Given that we know that the volume of a sphere of radius  $R$  is  $\frac{4}{3}\pi R^3$ , explain how the previous part can be used to deduce that the surface area of a sphere is given by  $S = 4\pi R^2$ .